



# Dzyaloshinskii-Moriya Interaction

You Spin me round...

Pierre Géhanne – IDMAG  
Cookies club – 14/06/2018

1. Magnetism : a short introduction
2. What is DMI ?
3. Effects of DMI

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# 1. Magnetism : a short introduction

- Back to basics



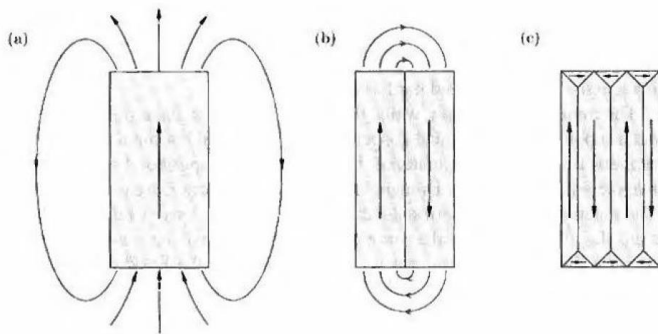
Iron...

- can be strongly magnetized
  - but not above a certain temperature  $T_c$
- A magnet cut in halves = two magnets

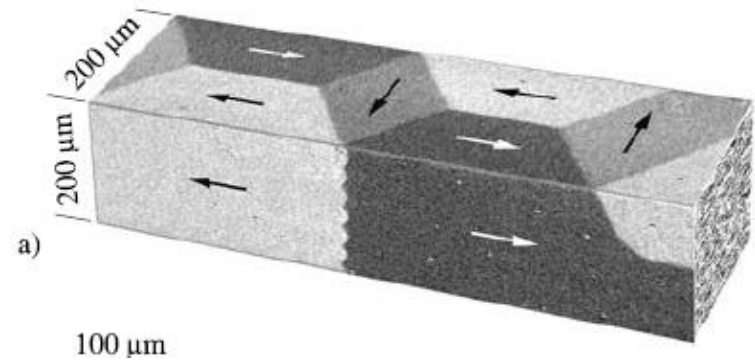
Some interaction holds microscopic magnets together  
-> exchange

How can a ferromagnet have zero magnetization under  $T_c$  ?

-> domains



Blundell (Oxford, 2001)



Hubert & Schäffer (Springer, 2009)

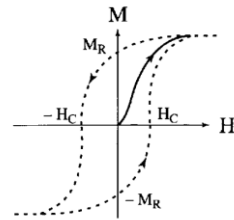
Magnetic domains

Heisenberg exchange  
(spins // to each other)

Dipole-dipole interaction  
(stray field cost energy)

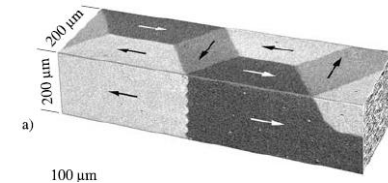
# 1. Magnetism : a short introduction

- The many scales of magnetism

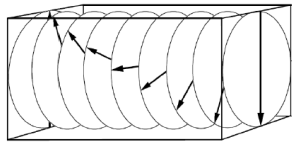


Macroscopic magnetism

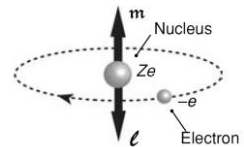
Domains ( $> 1 \mu\text{m}$ )  
Mesoscopic arrangement of magnetization



Domain walls ( $1 \text{ nm}$  to  $1 \mu\text{m}$ )  
Boundaries between areas of same magnetization



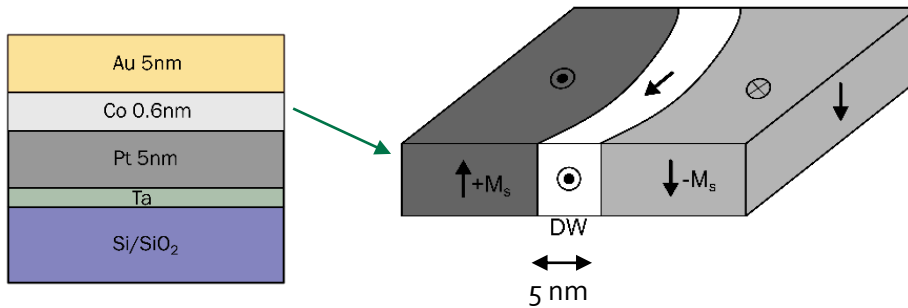
Atomic level ( $< 1 \text{ nm}$ )  
Elementary magnetic moments (localized or travelling electrons)



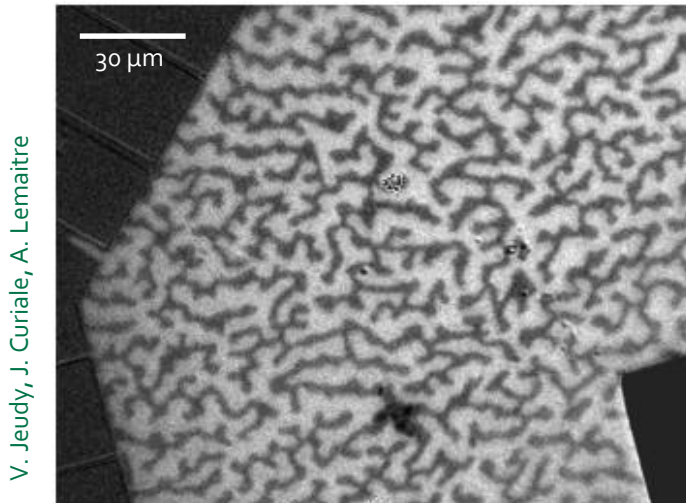
# 1. Magnetism : a short introduction

- Thin-films basics

## Magnetism of nearly 2D magnets :

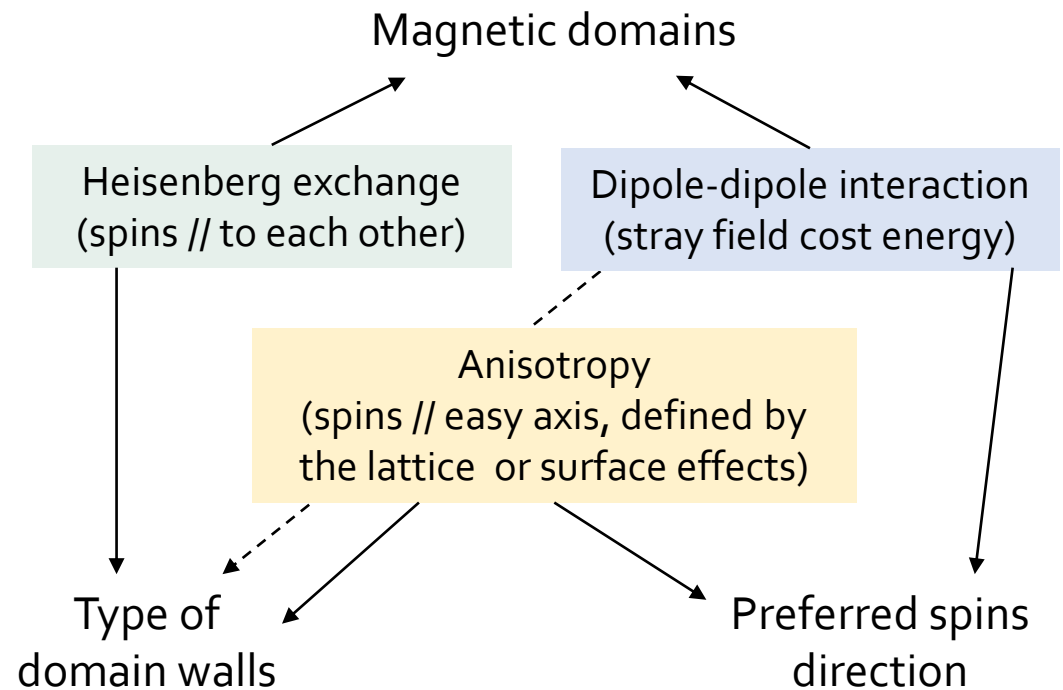


**Thin film** = A few mono layers of FM on top of a substrate, possibly sandwiched between other metals or oxydes.



V. Jeudy, J. Curiale, A. Lemaitre

Stripe domains in (Ga,Mn)/As (MOKE microscopy)



1. Magnetism : a short introduction
2. What is DMI ?
3. Effects of DMI



## 2. What is DMI ?

- Exchange : symmetric

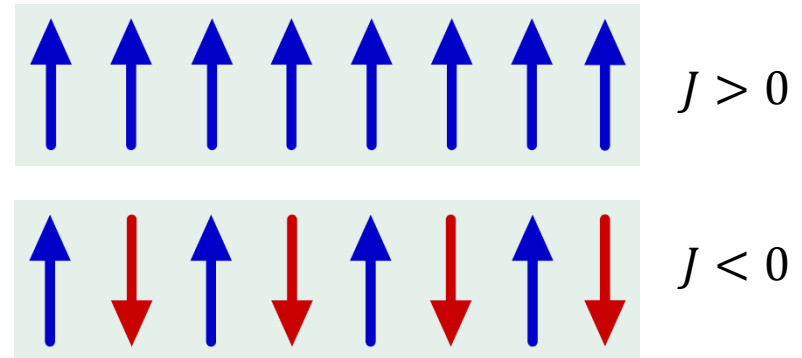
Exchange interaction :

$$H = \sum_{\langle i,j \rangle} \underbrace{-J \vec{S}_i \cdot \vec{S}_j}_{\text{Heisenberg}}$$

Heisenberg term (symmetric) :  
favors parallel spins

$J > 0$  Ferromagnetic order

$J < 0$  Antiferromagnetic order





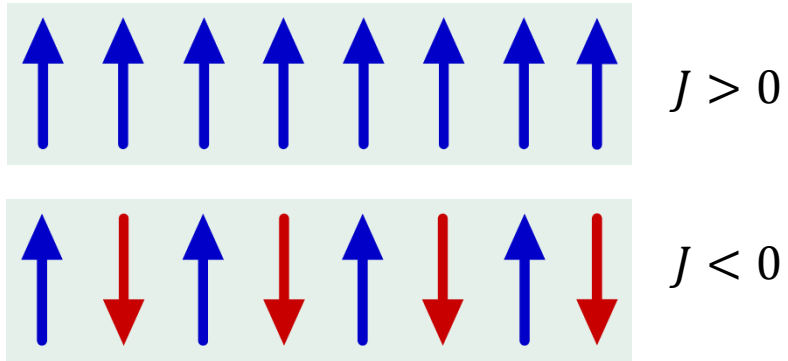
# 2. What is DMI ?

- Exchange : symmetric and antisymmetric

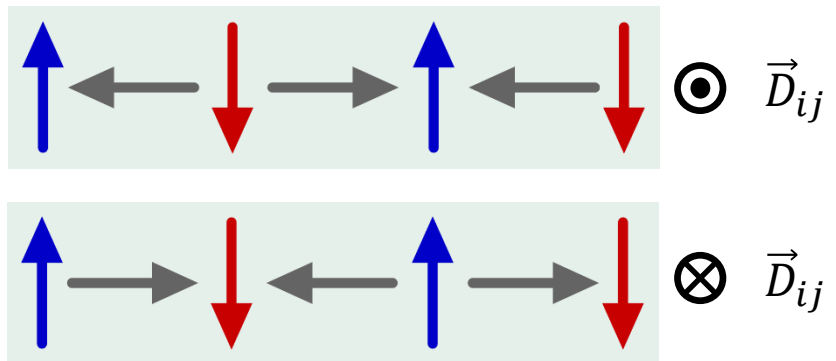
Exchange interaction :

$$H = \sum_{\langle i,j \rangle} \left[ \underbrace{-J \vec{S}_i \cdot \vec{S}_j}_{\text{Heisenberg}} + \underbrace{\vec{D}_{ij} \cdot (\vec{S}_i \times \vec{S}_j)}_{\text{DMI}} \right]$$

Heisenberg term (symmetric) :  
 favors parallel spins  
 $J > 0$  Ferromagnetic order  
 $J < 0$  Antiferromagnetic order



Dzyaloshinskii-Moriya term (antisymmetric) :  
 favors perpendicular spins.  
 The spins curl around the D vector,  
 whose direction depends on the sign of  
 the spin-orbit coupling and on the  
 geometry.



## 2. What is DMI ?

- History of DMI

In the 50's : some antiferromagnets display a small macroscopic magnetization... (e.g. hematite,  $\alpha\text{-Fe}_2\text{O}_3$ ).

**Dzyaloshinskii** : some canting of the spins is allowed if there is no inversion symmetry in the crystal

-> asymmetric term  $\vec{D}_{ij} \cdot (\vec{S}_i \times \vec{S}_j)$

**Moriya** : precise rules of symmetry to have  $\vec{D} \neq \vec{0}$  and two-site model based on superexchange to calculate its value.

**Fert & Levy** : 3-site model based on RKKY interaction with Spin-Orbit Coupling

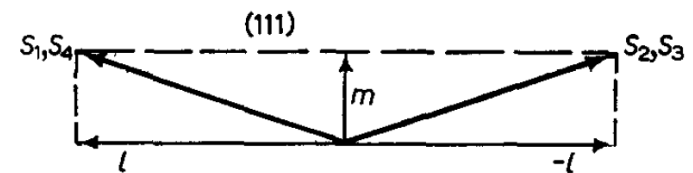


FIG. 2. Projection of ion spins on (1) for  $\alpha\text{-Fe}_2\text{O}_3$ .

Dzyaloshinskii, J.Phys.Chem.Solids (1958)  
Moriya, Phys.Rev. (1960)  
Fert & Levy, Phys.Rev.Lett. (1980)

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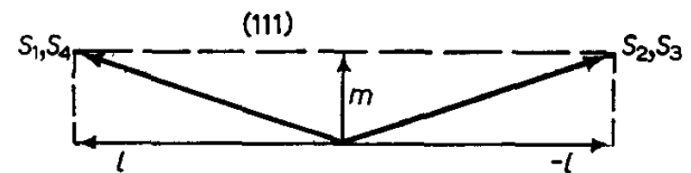


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*For theoreticians only!*

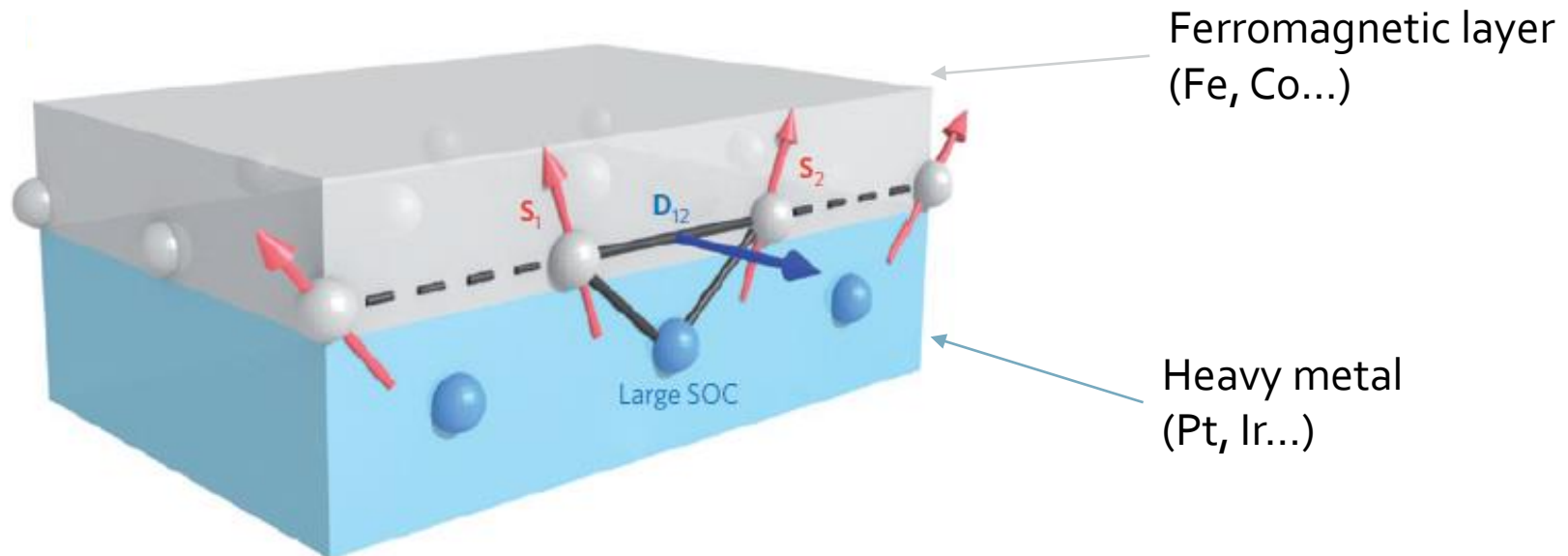
## 2. What is DMI ?

- It's always better with a picture

DMI appears only when inversion symmetry is broken :

- Low-symmetry lattices
- Surface and interfaces

Interfacial DMI :

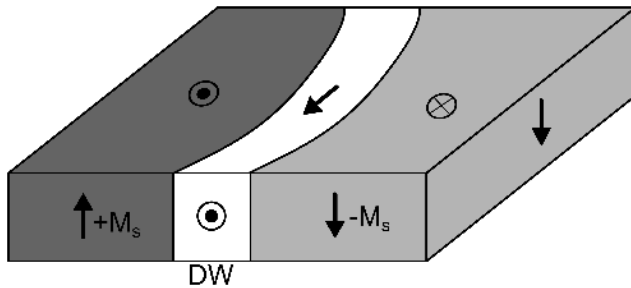


Fert et al., Nat.Nano. (2013)

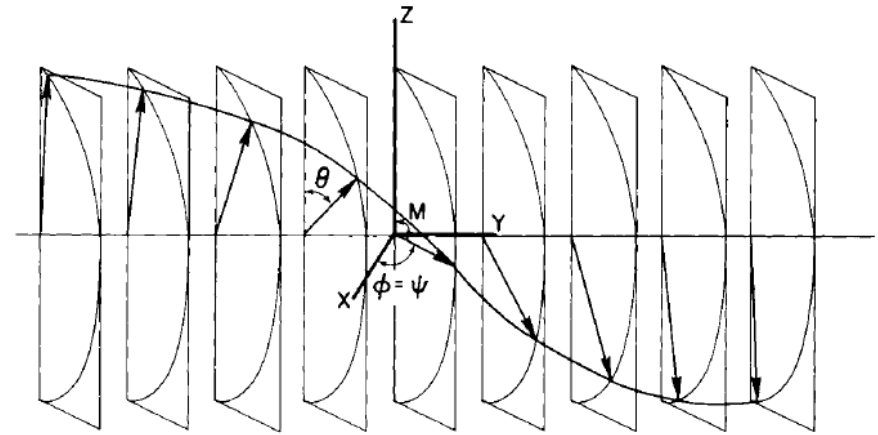
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### 3. Effects of DMI

- Domains walls



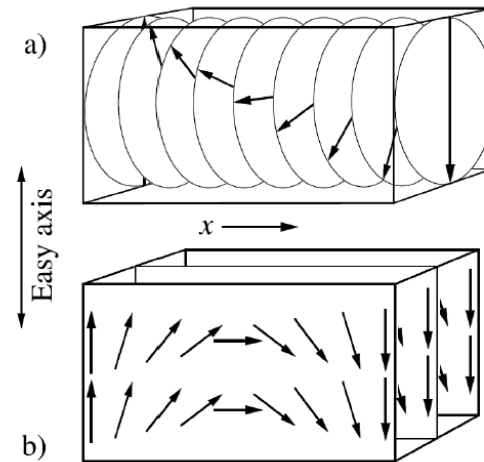
Domain wall = transition from an up to a down domain  
Size  $\approx 10$  nm



Malozemoff & Sloncewski (A.P. 1979)

Without DMI : the Bloch wall minimizes the stray field

With DMI : If  $D$  is larger than the stray field energy, Néel wall with a fixed chirality



Hubert & Schäffer (Springer, 2009)

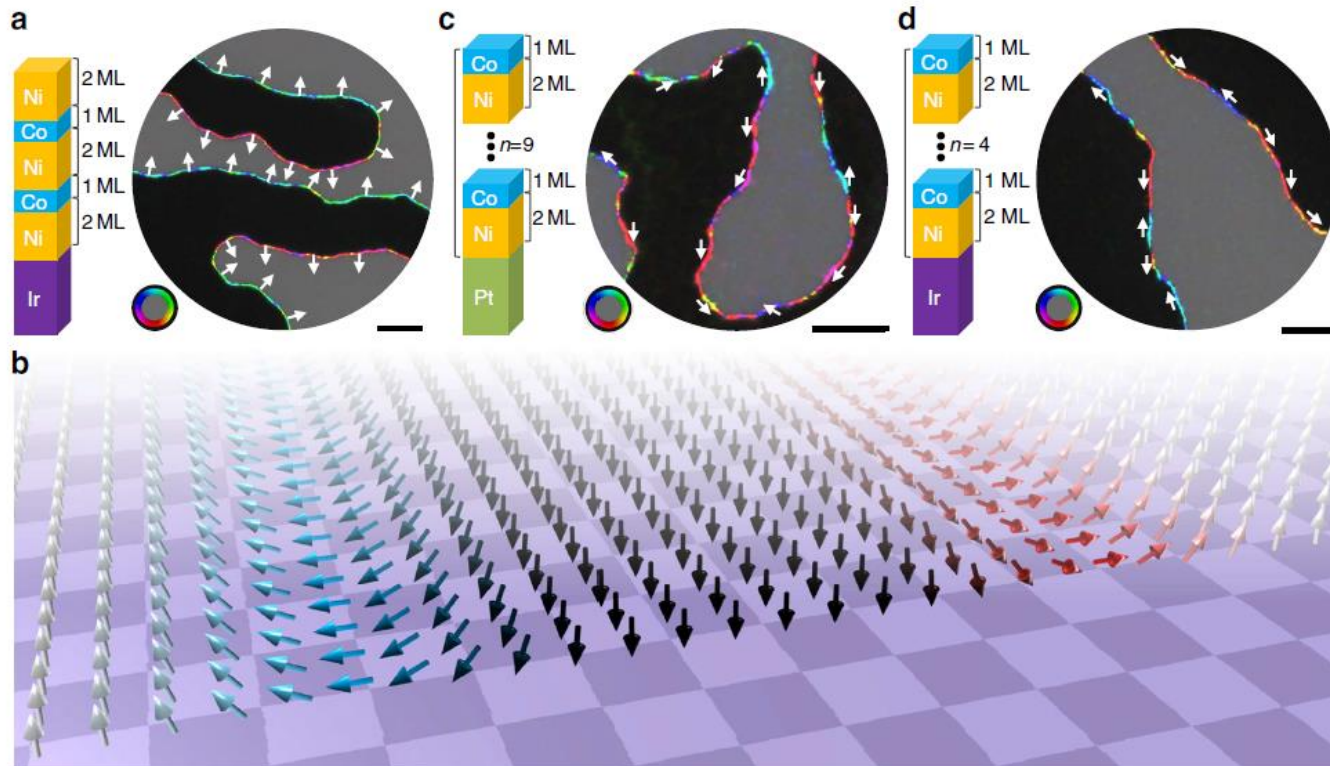
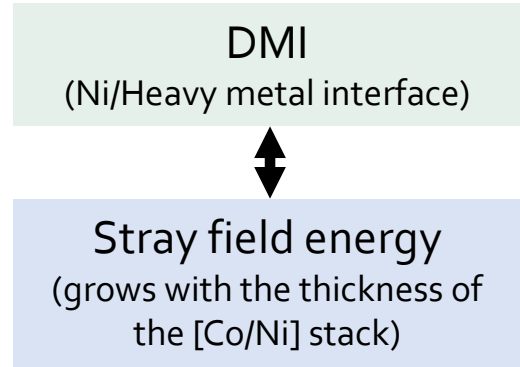
Parois de Bloch (a) et de Néel (b).

# 3. Effects of DMI

- Dzyaloshinskii Domain Walls

Chen *et al.*, Nat.Com. (2013) : Tailoring the chirality of magnetic DW by interface engineering

SP-LEEM observation of  $[\text{Co}/\text{Ni}]_n$  stacks on Pt or Ir

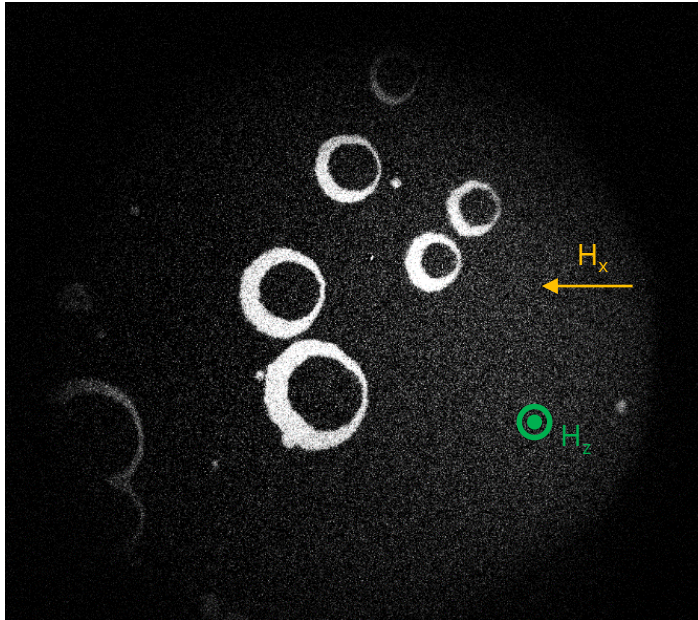




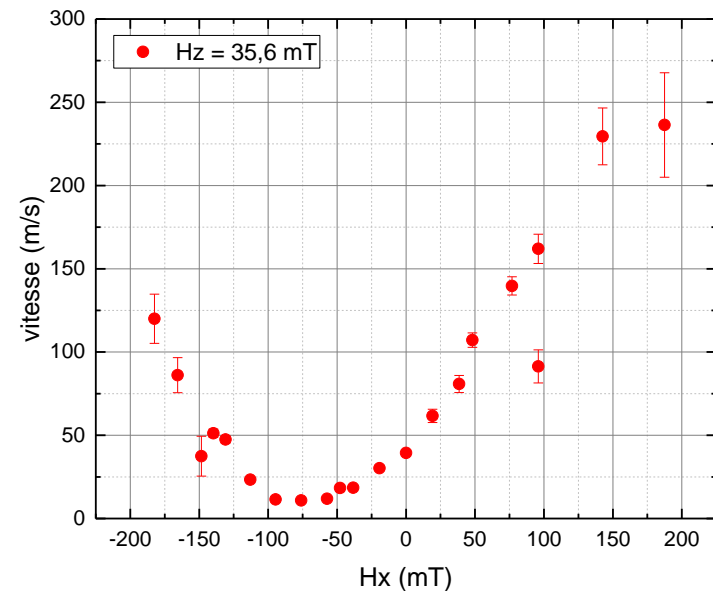
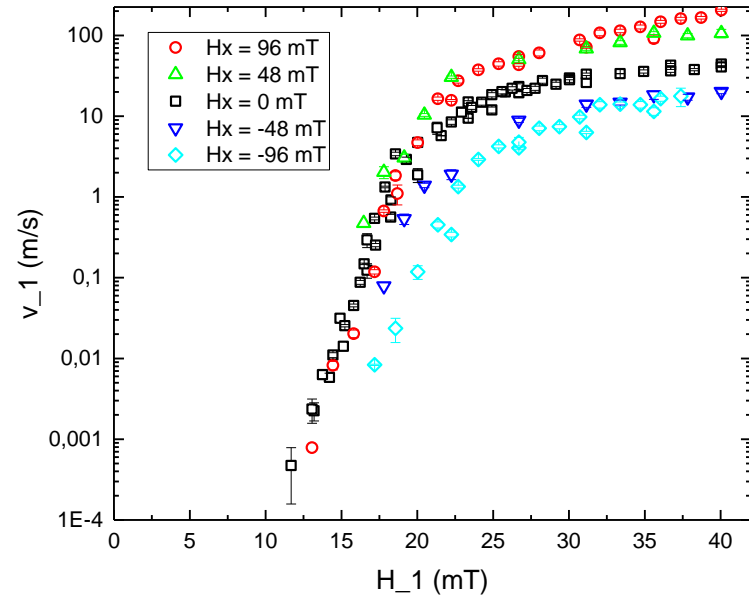
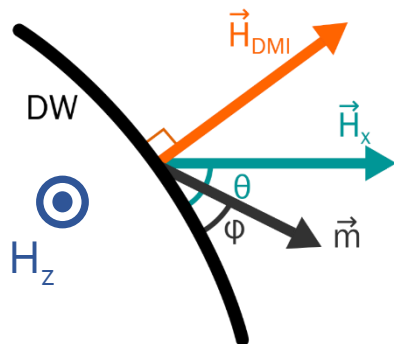
# 3. Effects of DMI

- DDW dynamics

Motion of Dzyaloshinskii domain walls

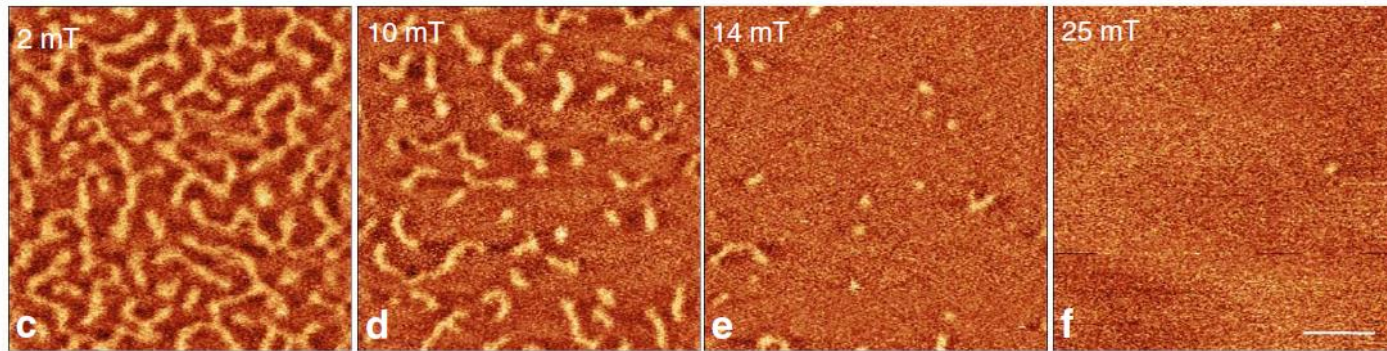


Asymmetric domain growth in Pt/Co/Au



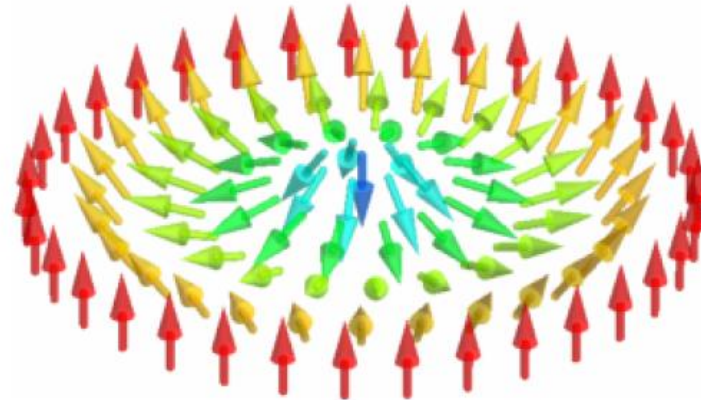
### 3. Effects of DMI

- Skyrmions



Hrabec *et al.* Nat.Com. (2017) Stabilization of isolated hedgehog skyrmions in Pt/Co/Au/Co/Pt, observed by MFM.

Hedgehog skyrmion  
= Néel wall loop



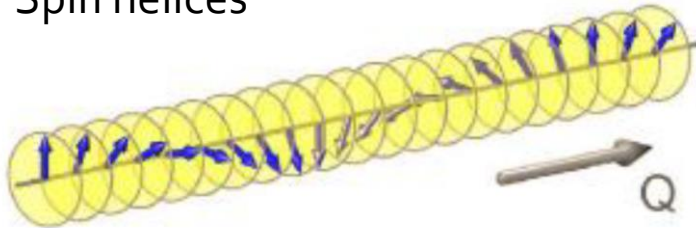
Everschor, PhD thesis (2012)

### 3. Effects of DMI

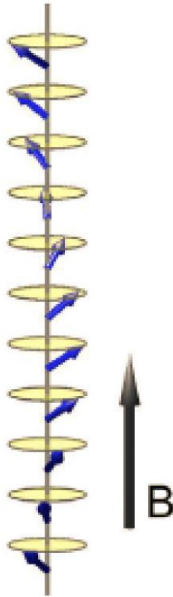
- Bulk chiral magnetic phases : MnSi

The interplay between Heisenberg exchange and DMI give rise to 3D chiral magnetic structures

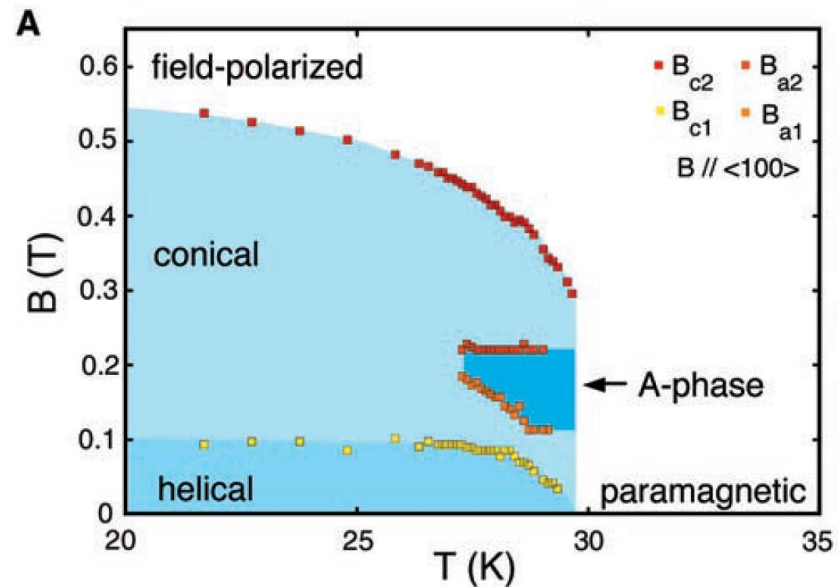
Spin helices



Conical helices



Mühlbauer *et al.*, *Science* (2011) :  
Phase diagram of MnSi under a magnetic field (neutron diffraction)

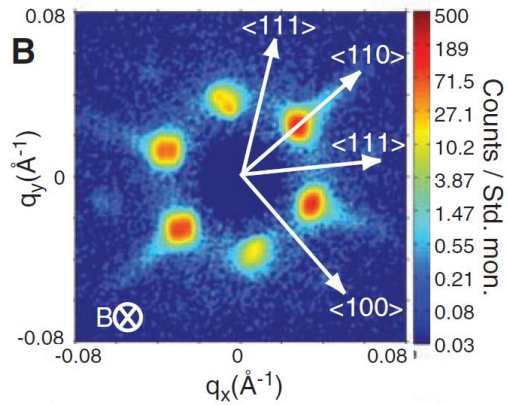




### 3. Effects of DMI

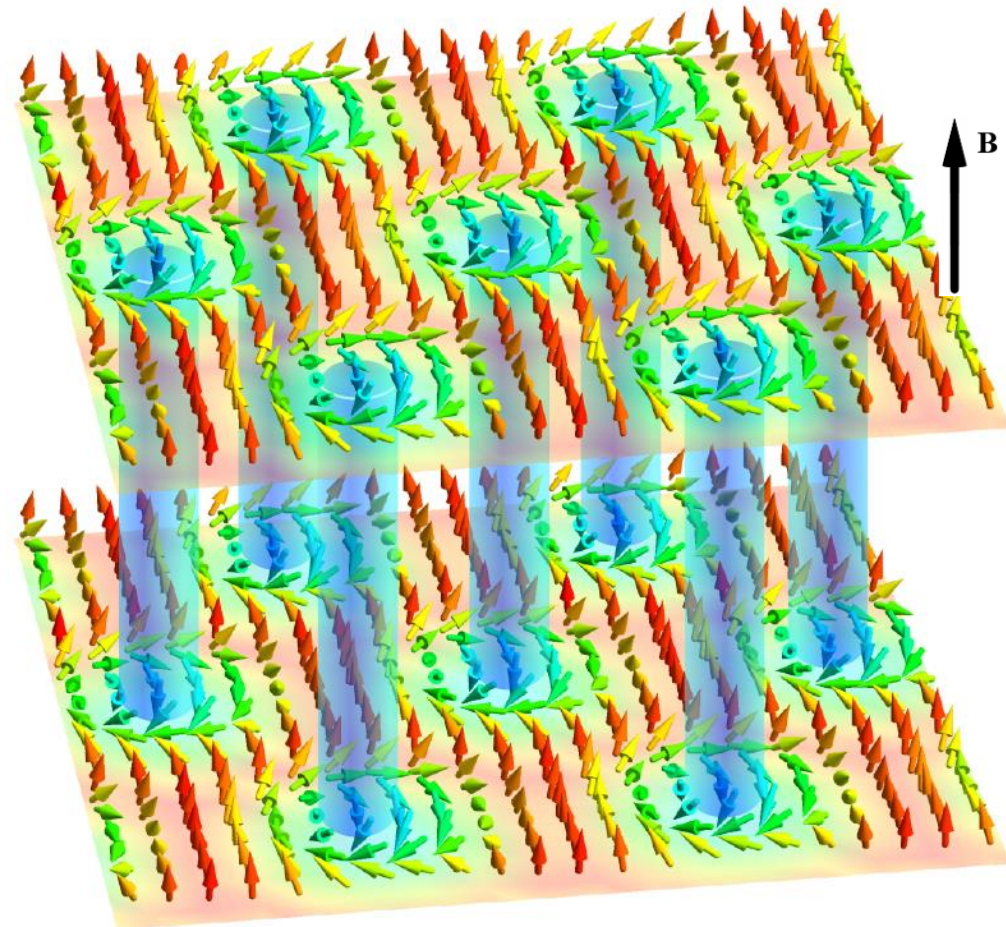
- Bulk chiral magnetic phases : MnSi

A-phase : 6-fold symmetry -> Skyrmion lattice

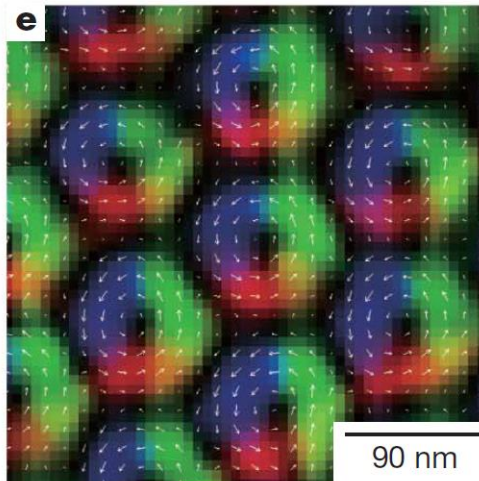


Mühlbauer *et al.*, Science (2009)

B2o cubic lattice constant :  $a = 4.56 \text{ \AA}$   
Skyrmion lattice constant :  $\lambda = 190 \text{ \AA}$



Observed in real space by Lorentz TEM  
on  $\text{Fe}_{0.5}\text{Co}_{0.5}\text{Si}$



Yu *et al.*, Nature (2010)

14/06/2018

Everschor, PhD thesis (2012)

The end !

# More slides

- Micromagnetism of thin-films

Micromagnetism = mesoscopic description of spin configurations and dynamics

Individual spins  $\vec{S}_i$   $\xrightarrow{\text{Average over a few nm}}$  Local magnetization  $\vec{M} = M_S \vec{m}$

Heisenberg exchange :

$$H = -J \sum_{\langle i,j \rangle} \vec{S}_i \cdot \vec{S}_j \quad \longrightarrow \quad e_{ex} = A \int [(\vec{\nabla} m_x)^2 + (\vec{\nabla} m_y)^2 + (\vec{\nabla} m_z)^2] dV$$

Dipole-dipole interaction and anisotropy  $\longrightarrow e_K = K_{eff} (\vec{m} \cdot \vec{e}_K)^2 + \text{higher order terms}$

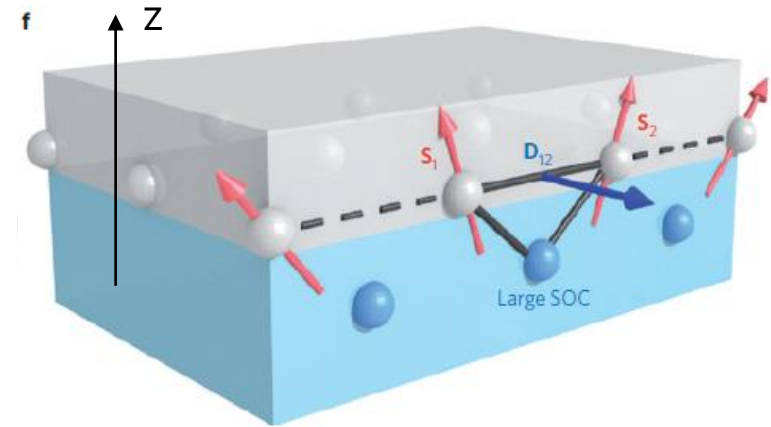
# More slides

- Micromagnetism of thin-films

Interface between a ferromagnet and a heavy metal

$$\vec{D}_{ij} = D \hat{u}_{ij} \times \hat{u}_z$$

D lies in the plane of the interface



$$H_{DMI} = \sum_{\langle i,j \rangle} \vec{D}_{ij} \cdot (\vec{S}_i \times \vec{S}_j)$$

$$\rightarrow e_{DMI} = D_S \left[ \left( m_x \frac{\partial m_z}{\partial x} - m_z \frac{\partial m_x}{\partial x} \right) + \left( m_y \frac{\partial m_z}{\partial y} - m_z \frac{\partial m_y}{\partial y} \right) \right]$$

Rohart *et al.*, Phys.Rev.B (2013)